

# 异质固-液界面台阶自由能的计算研究

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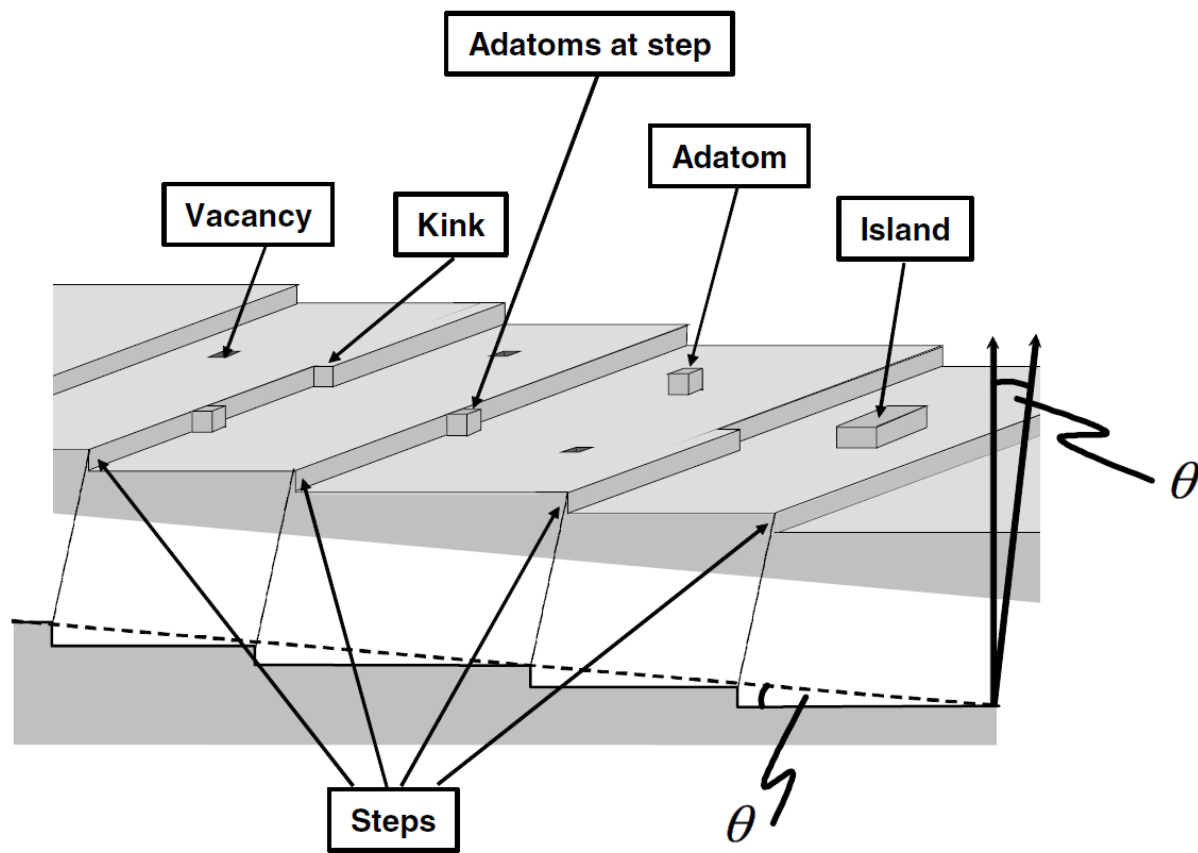
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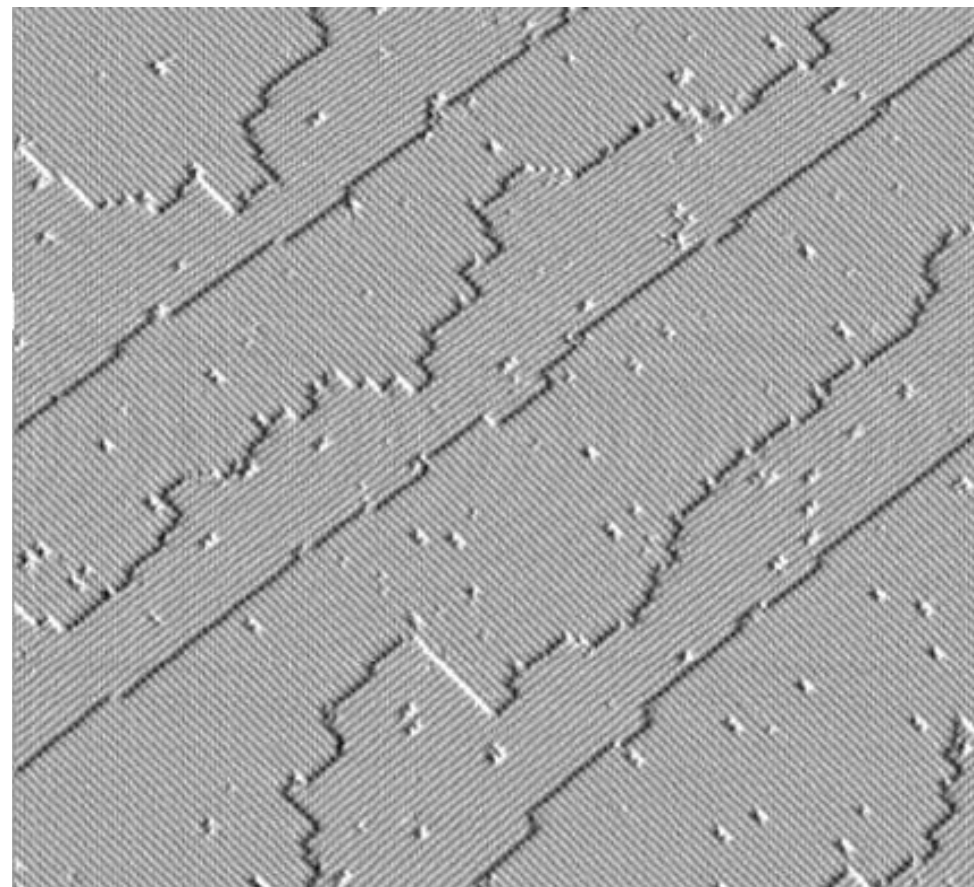
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# 1、研究背景：台阶，台阶自由能



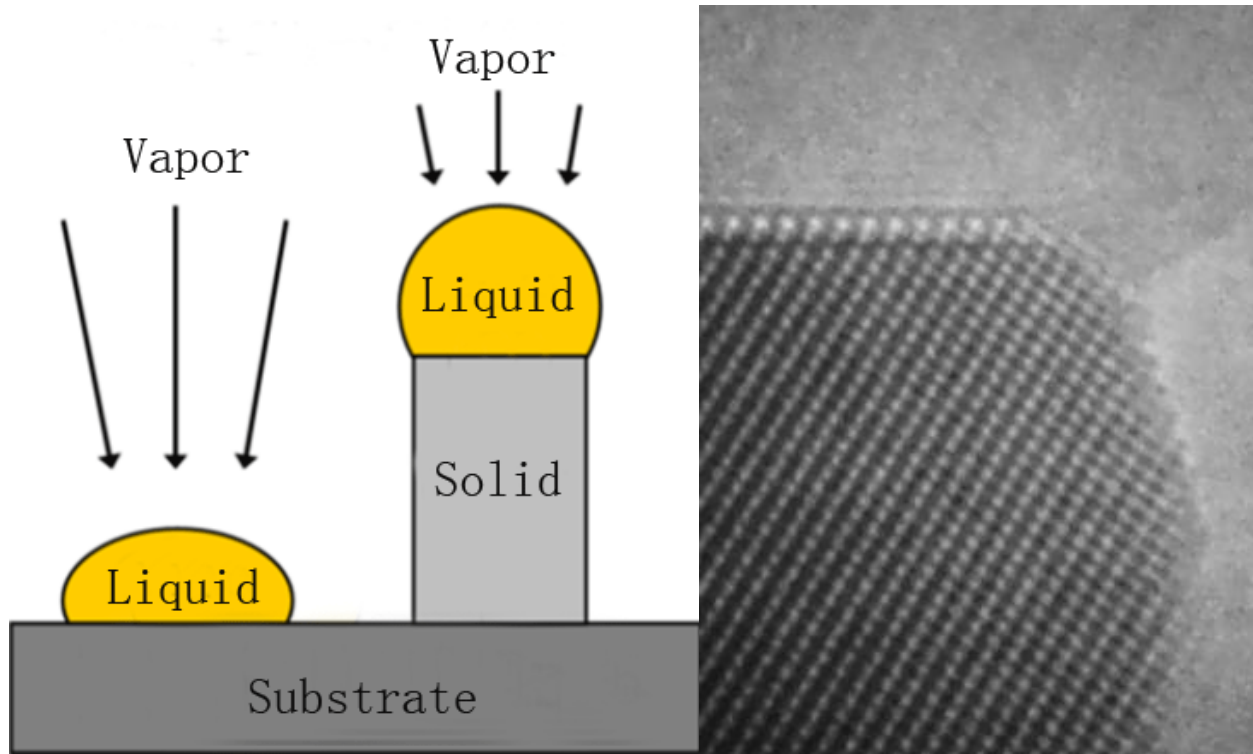
固体表面示意图



Si (100) 表面STM图

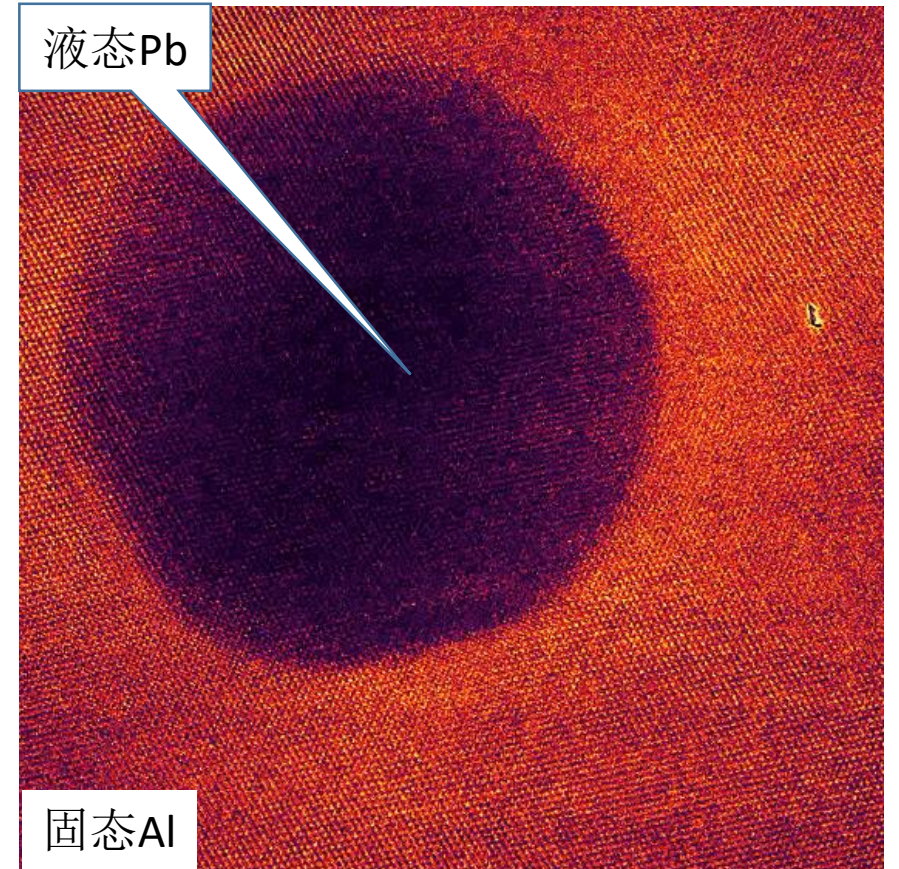
台阶自由能是表征形成长度单位台阶难易程度的物理量。

# 1、研究背景:台阶自由能的研究意义



纳米材料在纳米器件以及催化作用等方面具有很大的应用，其中在VLS一层一层生长晶须过程中，形成台阶是整个过程的第一步。

*Sang Ho Oh et al, Science. 489,93(2010)*

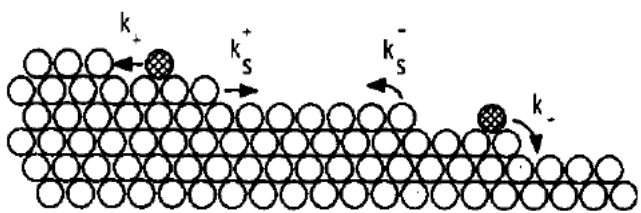


在异质固液界面成核理论中，台阶自由能的大小将影响成核的大小等。以及液态杂质在固体中的迁移速度等。

*E. Johnson et al., J. Mater. Sci. (2005), and  
Privately provided by Uli Dahmen.*

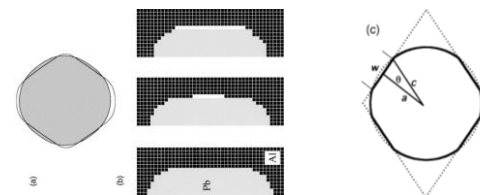
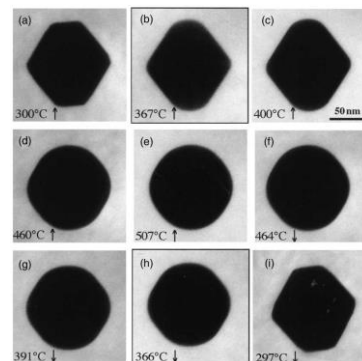
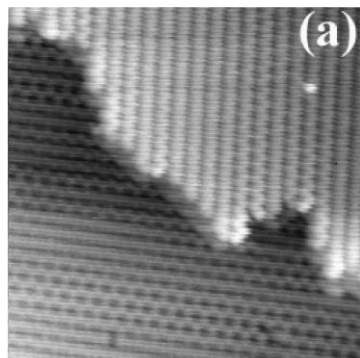
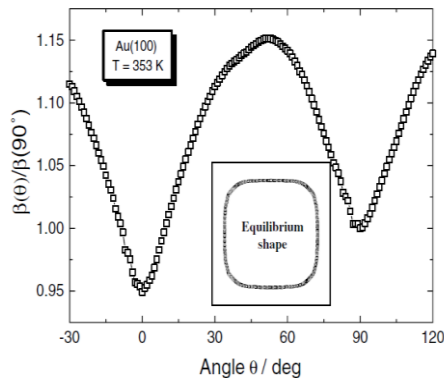
# 1、研究背景:台阶自由能的计算方法

70年代左右



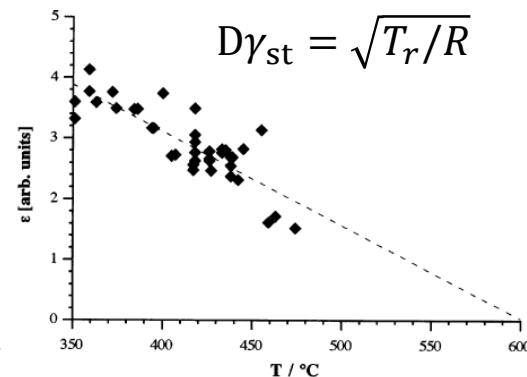
**Richard L. Schwoebel, Journal of Applied Physics, 49, 2 (1969)**

2000年左右



$$\Delta G(r) = 2\pi r \gamma_{st} - \pi r^2 h \Delta G_{vol}$$

$$D\gamma_{st} = \sqrt{T_r/R}$$



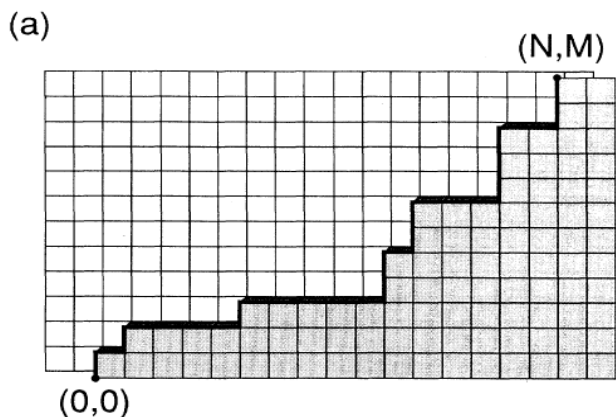
$$\frac{\gamma_{st}}{\gamma_{Al/Pb}} = h \sqrt{1 - \frac{a^2}{c^2}}$$

$$T = 623K;$$

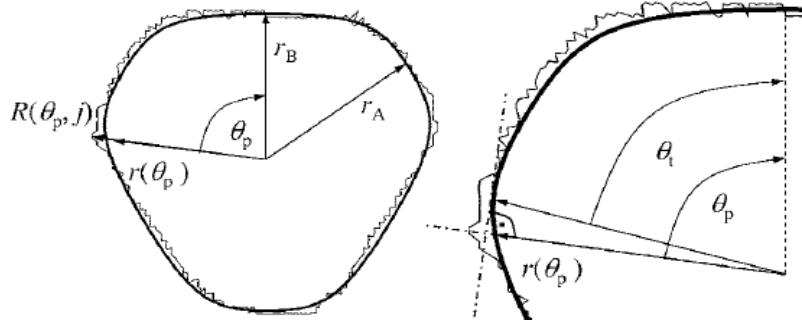
$$\gamma_{st} = 0.19 \times 10^{-10} J/m$$

solid-on-solid model

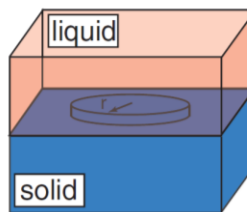
**G Bilalbegovic, J. Phys. A: Math. Gen. 22, L833-L836 (1989)**



**Ch. Bombis and H. Ibach, Surface Science 564, 201-210 (2004)**  
**H. J. W. Zandvliet, PHYSICAL REVIEW B 75, 9972 (2000)**

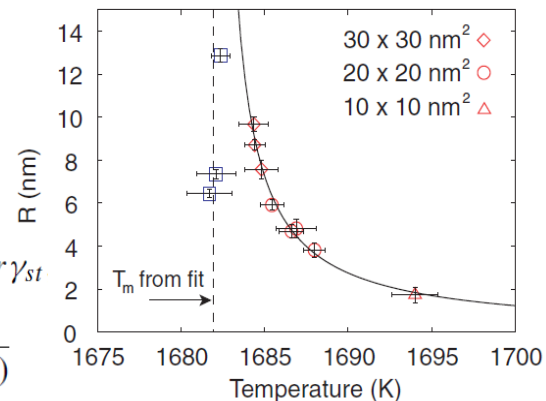


**H. Gabrisch, L. Kjeldgaard, E. Johnson and U. Dahmen, Acta mater. 49, 4259 (2001)**



$$G = -\Delta\mu\rho_A\pi r^2 + 2\pi r\gamma_{st}$$

$$R = \frac{\gamma_{st} T_m}{\rho_A H_m (T_m - T)}$$



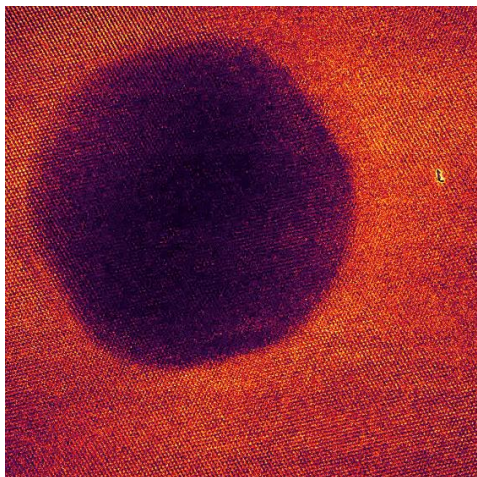
**Julian Ikonov, Kirilka Starbova, and Harald Ibach, PHYSICAL REVIEW B 75, 245411 (2007)**

$$\gamma_{st} = 0.103 \pm 0.005 \times 10^{-10} J/m$$

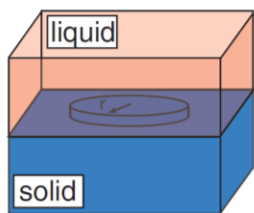
**T. Frolov and M. Asta, J.Chem.Phys. 137, 214108 (2012)**

**Mark Holzer and Michael Wortis, PRB, 40, 11044 (1989)**

## 2、研究动机和理论基础

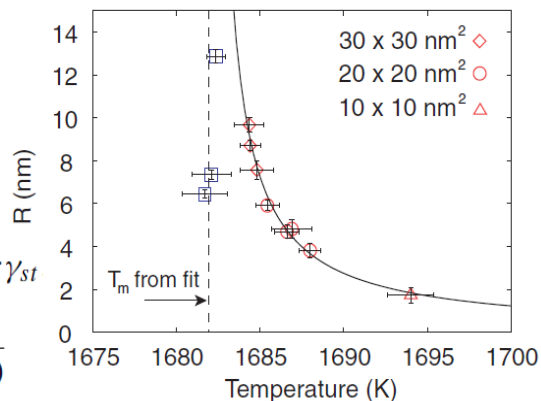


*E. Johnson et al., J. Mater. Sci. (2005), and Privately provided by Uli Dahmen.*



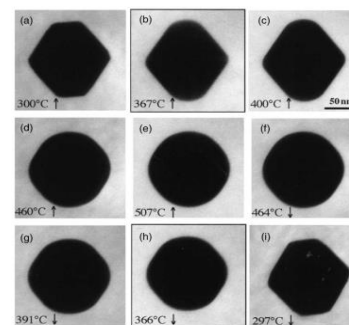
$$G = -\Delta\mu\rho_A\pi r^2 + 2\pi r\gamma_{st}$$

$$R = \frac{\gamma_{st}T_m}{\rho_A H_m(T_m - T)}$$



$$\gamma_{st} = 0.103 \pm 0.005 \times 10^{-10} \text{ J/m}$$

*T. Frolov and M. Asta, J.Chem.Phys. 137,214108(2012)*

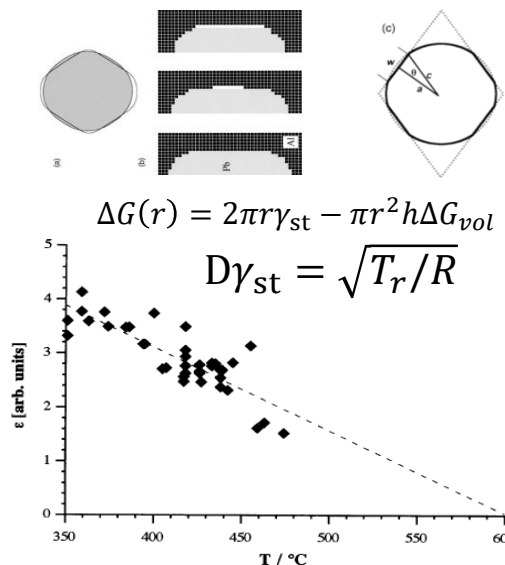


$$\frac{\gamma_{st}}{\gamma_{Al/Pb}} = h \sqrt{1 - \frac{a^2}{c^2}}$$

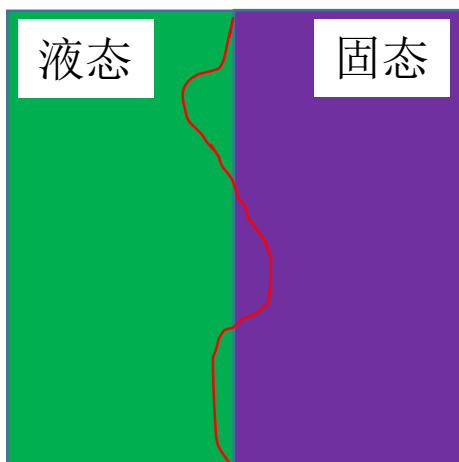
$$T = 623\text{K};$$

$$\gamma_{st} = 0.19 \times 10^{-10} \text{ J/m}$$

*H.Gabrisch, L.Kjeldgaard, E.Johnson and U. Dahmen, Acta mater. 49,4259(2001)*



目标：使用分子动力学模拟结合一种直接测量方法计算Al-Pb体系固液界面台阶自由能。



$$H = \gamma_{st} \int \left[ \sqrt{1 + (\nabla \xi(x))^2} - 1 \right] dx$$

$$\xi(x) = \sum_{q \neq 0} \widehat{\xi}_q \exp(iqx)$$

$$H = \frac{1}{2} \gamma_{st} L_x \sum_{q \neq 0} q^2 |\widehat{\xi}_q|^2$$

$$\langle |\widehat{\xi}_q|^2 \rangle = \frac{k_B T}{L_x \gamma_{st} q^2}$$

试图将毛细波理论方法拓展到固液界面台阶体系中。

# 5、研究方法和模拟细节

使用LAMMPS模拟；时间步长：2fs；模拟时长：50ns；相互作用势：EAM；温度：750K；

建立Al-Pb固液  
界面平衡态



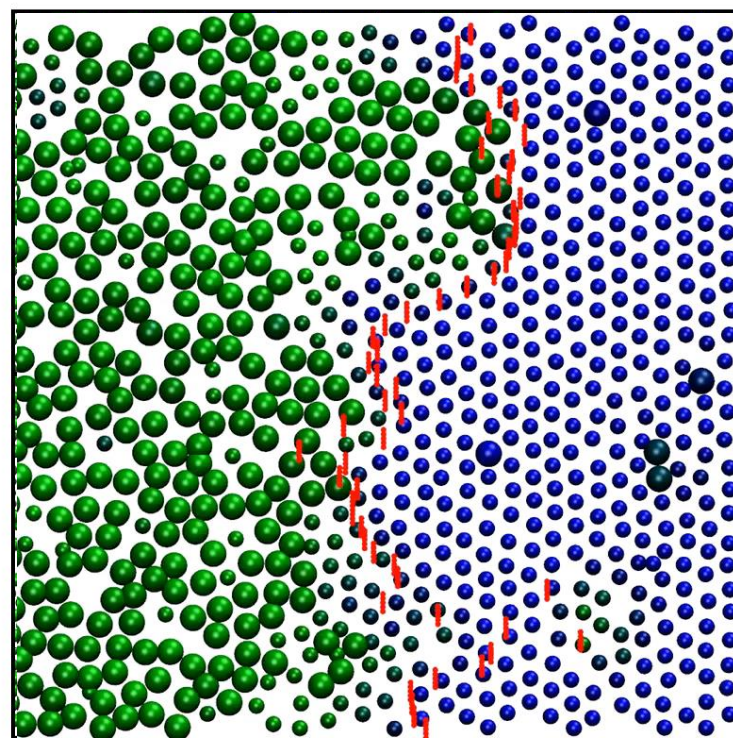
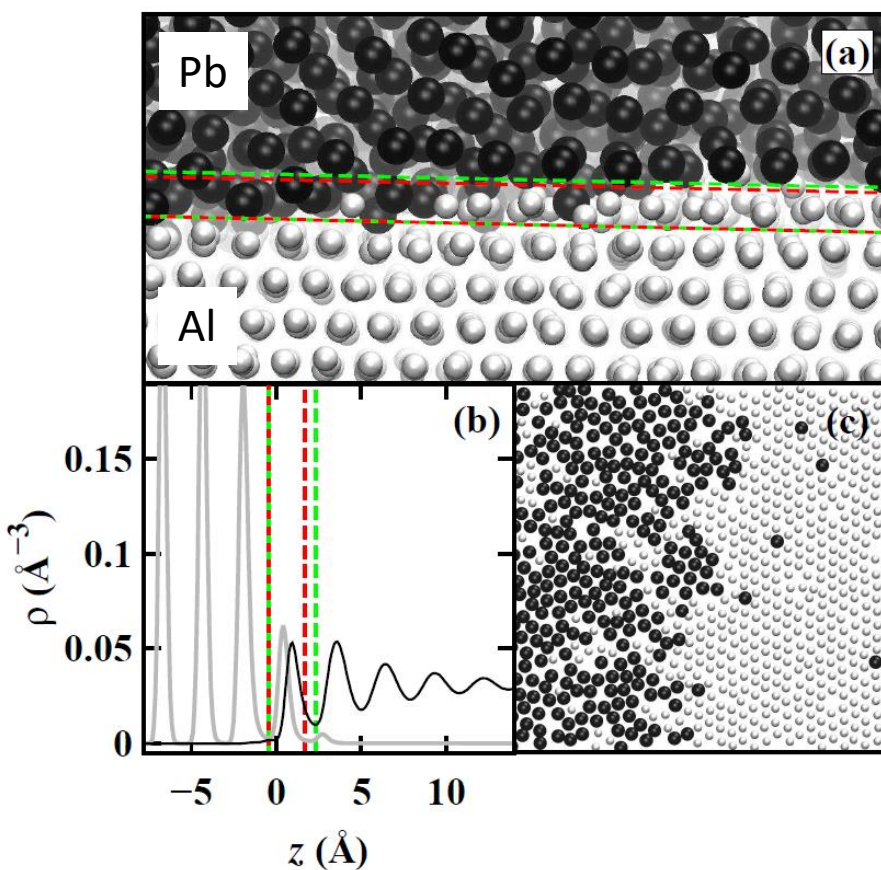
确定界面层位置



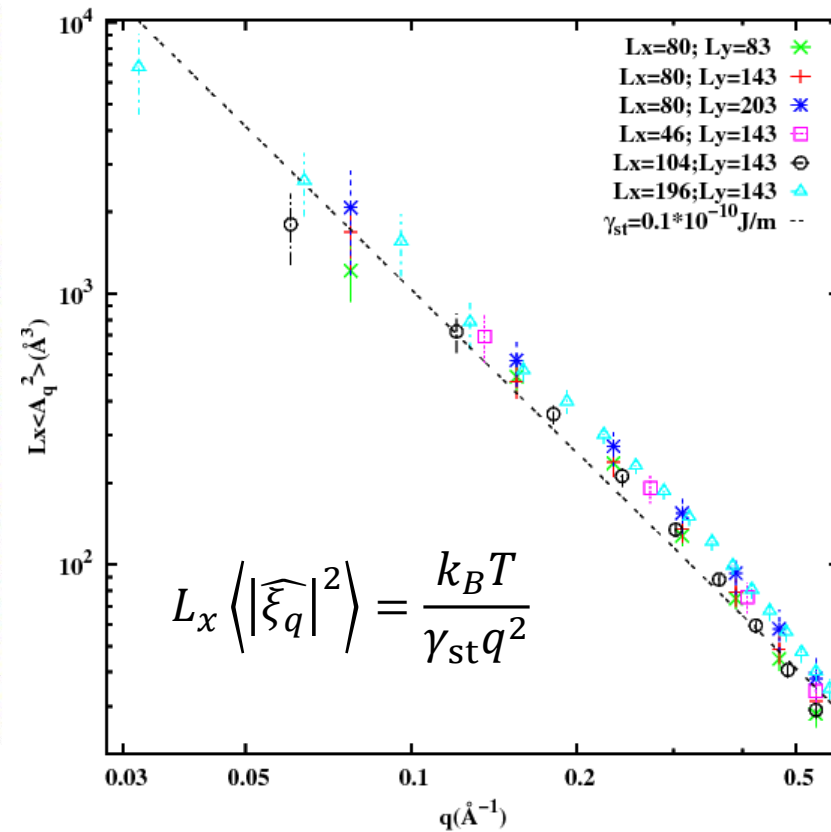
使用序参量方法确定台阶位置



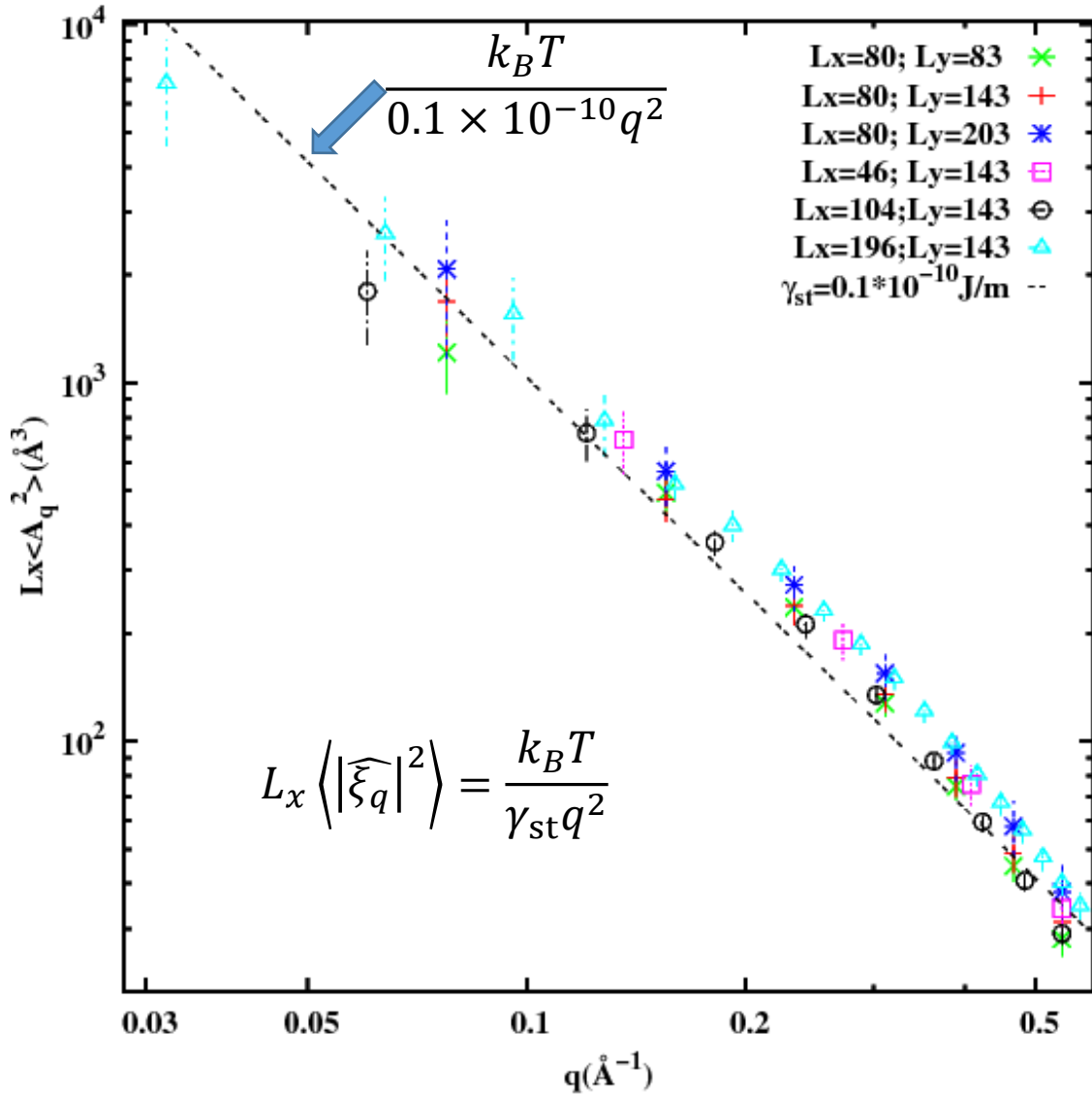
分析台阶震动谱，使用毛细  
波理论得出台阶自由能



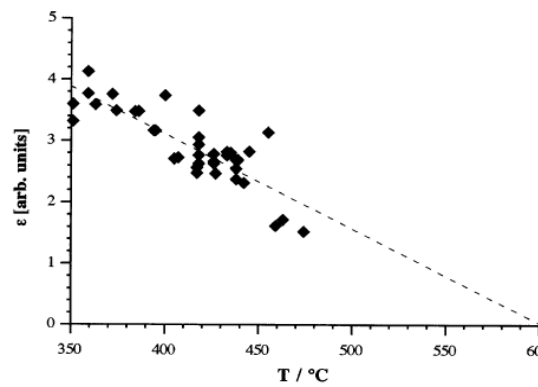
$$\varphi = \left| \frac{1}{N_b} \frac{1}{Z} \sum_r \sum_b \exp(i\vec{b} \cdot \vec{r}) \right|^2$$



# 6、模拟结果



体系	原子数	Lx(Å)	Ly(Å)	$\gamma_{st}$ ( $10^{-10} \text{ J/m}$ )
A	42581	80	83	0.10(1)
B	73266	80	143	0.10 (2)
C	103906	80	203	0.09(2)
D	41883	46	143	0.08(1)
E	115168	127	143	0.11 (1)
F	177921	196	143	0.09 (1)
G	94205	104	143	0.10(1)
H	252899	277	143	0.11(2)



$T = 623\text{K}; \gamma_{st} = 0.19 \times 10^{-10} \text{ J/m}$   
 $T = 873\text{K}; \gamma_{st} = 0.0 \text{ J/m}$   
 $T = 750\text{K}; \gamma_{st} = 0.094 \times 10^{-10} \text{ J/m}$

*H.Gabrisch, L.Kjeldgaard, E.Johnson and U. Dahmen, Acta mater. 49,4259(2001)*



# 5、总结

- 本次报告首先介绍了台阶和台阶自由能，以及很多关于台阶自由能的研究。针对目前研究情况，我们研究了固液界面台阶体系。
- 由于实验技术的限制，我们采用分子动力学模拟，结合毛细波涨落方法成功的得到了Al-Pb体系固液界面的台阶自由能。
- 我们拓展了CFM的适用范围，验证了该方法适用于计算固液界面内的台阶自由能。该方法同样也适用于其它体系。

Thank You ! ! !