



# Efficient Self-Learning Techniques for SAT-Based Test Generation

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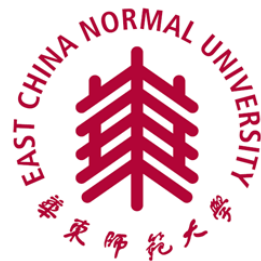
**Ang Li and Mingsong Chen**

*Shanghai Key Lab of Trustworthy Computing*

*East China Normal University, China*



**October 9, 2012**





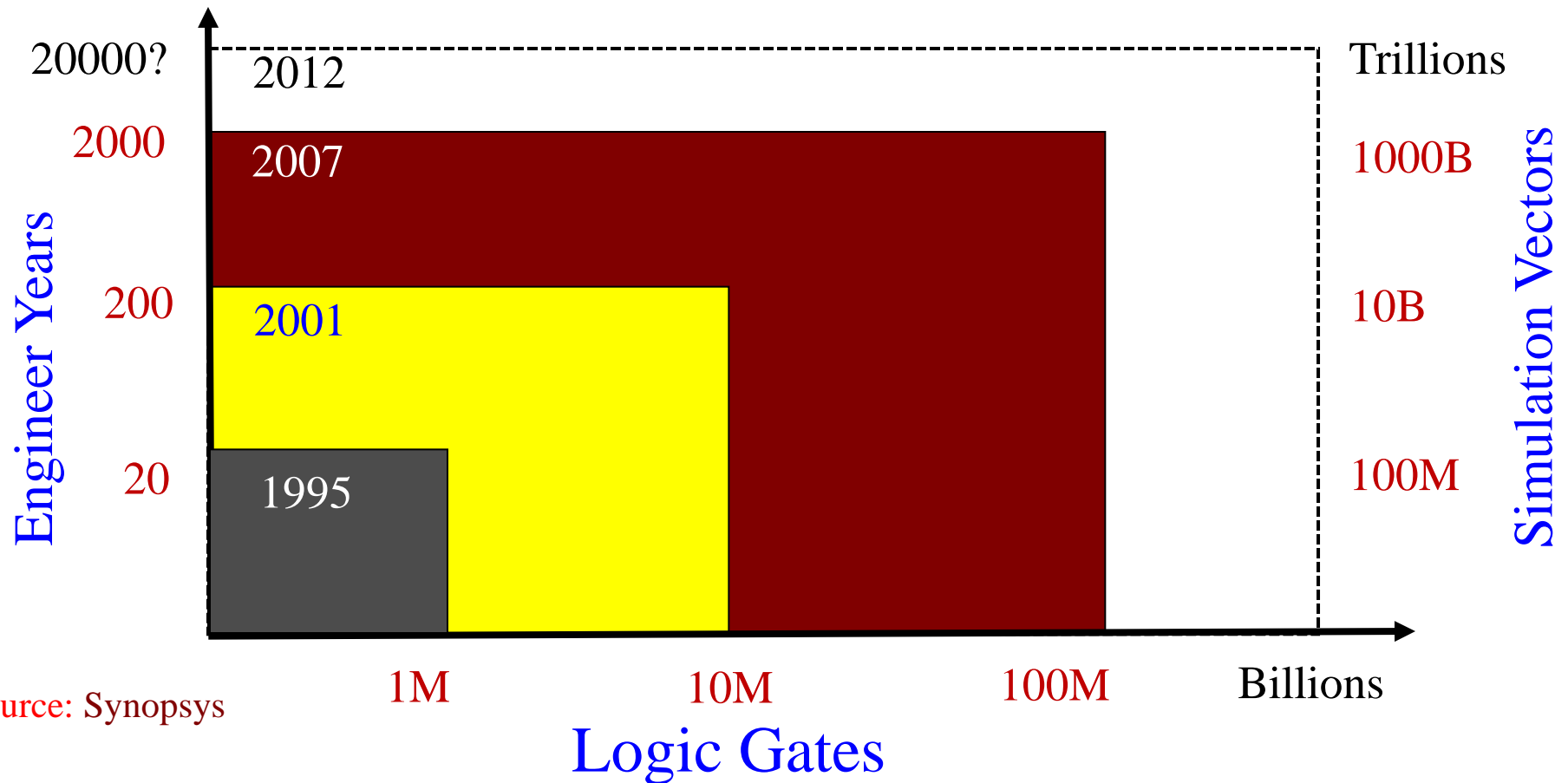
# Outline

- **Introduction**
- **SAT-Based Directed Test Generation**
  - **Test Generation using Model Checking**
  - **Test Generation using SAT-Based BMC**
- **Our Self-Learning Techniques**
  - **Motivation and Overview**
  - **Learning Oriented Partitioning Heuristics**
  - **Self-Learning Based Test Generation**
- **Experiments**
- **Conclusions**

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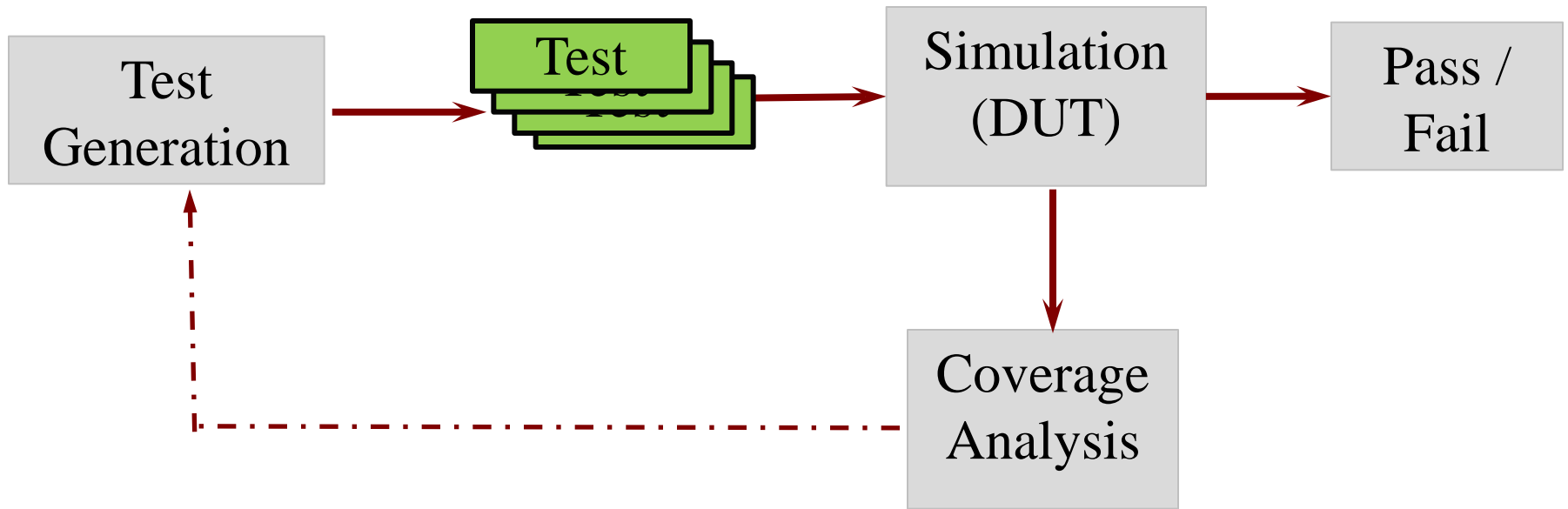
# Functional Validation of SoC Designs



Source: Synopsys

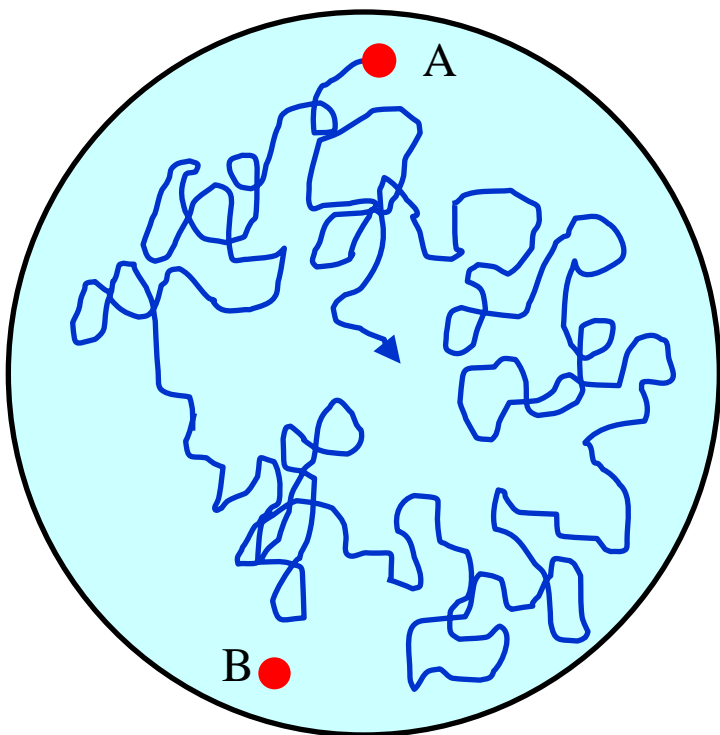
- SoC Validation is a major bottleneck
- ◆ Up to 70% time and resources are used!

# Simulation-based Validation

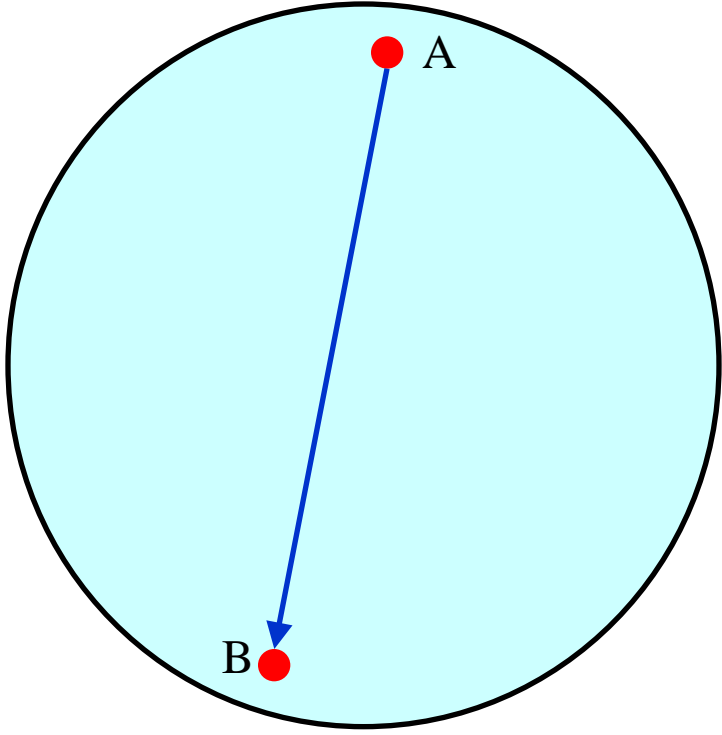


# Why Directed Test Generation

- Activate desired behavior with efficient tests



Random Test



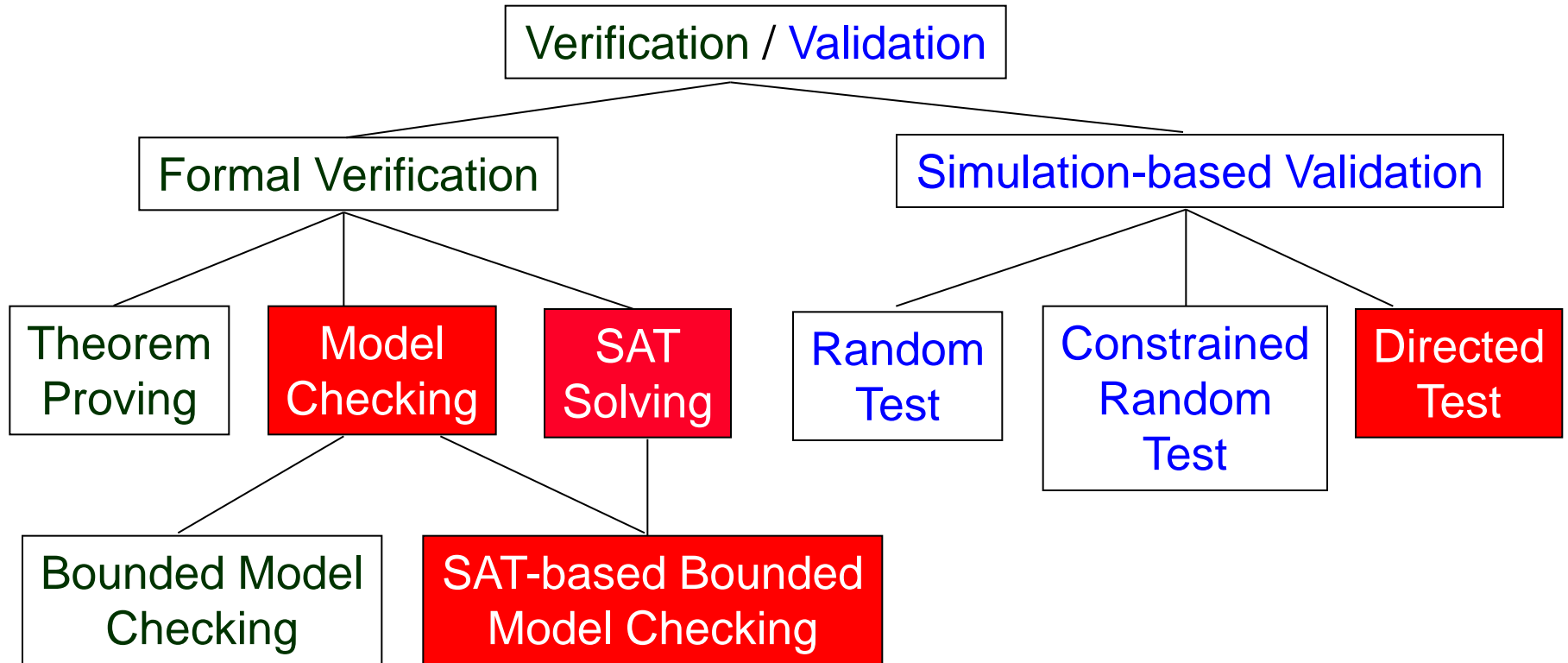
Directed Test

- Need for automated generation of directed tests

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# Automated Directed Test Generation

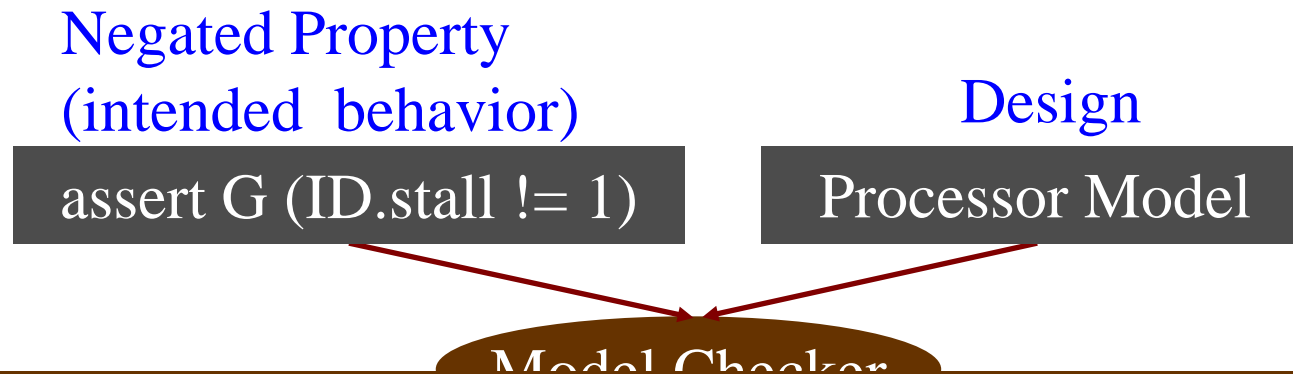


Directed test generation based on the automation of model checking techniques.



# Test Generation using Model Checking

Example: Generate a directed test to stall a decode unit (ID)



**Problem:** Test generation is very costly or not possible in many scenarios in the presence of complex SoCs and/or complex properties.

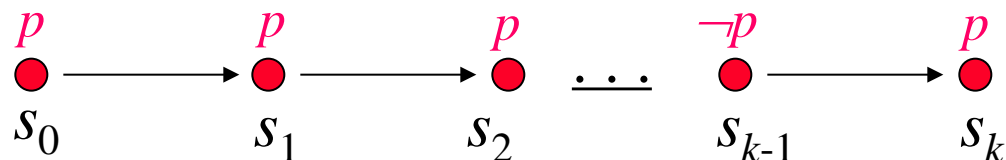
**Approach:** Exploit some learning to reduce complexity

- Reduce TG time & memory requirements
- Enable test generation in complex scenarios

# SAT-based Bounded Model Checking

- Test generation needs to consider **safety** properties
- The safety property  **$P$**  is valid up to cycle  **$k$**  iff  **$\Omega(k)$**  is not satisfiable.

$$\Omega(k) = I(S_0) \wedge \bigwedge_{i=0}^{k-1} R(S_i, S_{i+1}) \wedge \bigvee_{i=0}^k \neg P(s_i)$$



- If  **$\Omega(k)$**  is satisfiable, then we can get an assignment which can be translated to a **test**.

# DPLL Search Procedure

```
while (1){  
    run_periodic_function();  
    if( Decision ) {  
        while ( Deduction == CONFLICT ) {  
            blevel = Diagnosis ();  
            if( blevel < 0 )  
                return UNSAT;  
        }  
    } else return SAT;  
}
```

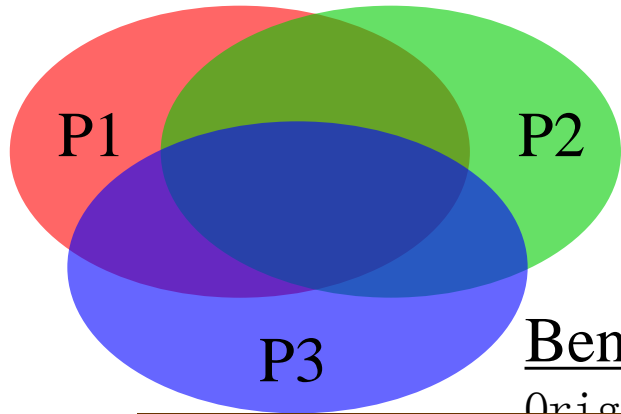
*SAT search time can be improved if we can reduce:*

- *the number of bad decisions at early stage, and*
- *the number of long distance backtracks.*

# Outline

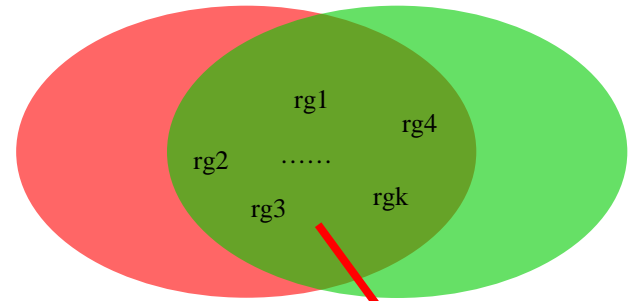
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# Property Learning Techniques



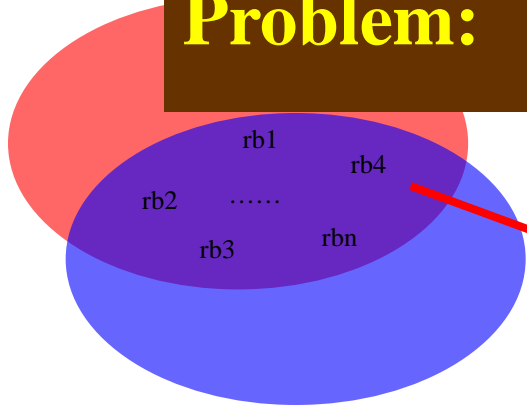
Benefit:

Original: Red + Blue + Green



Forward

**Problem:** There is a lack of learning for P1?



Forward

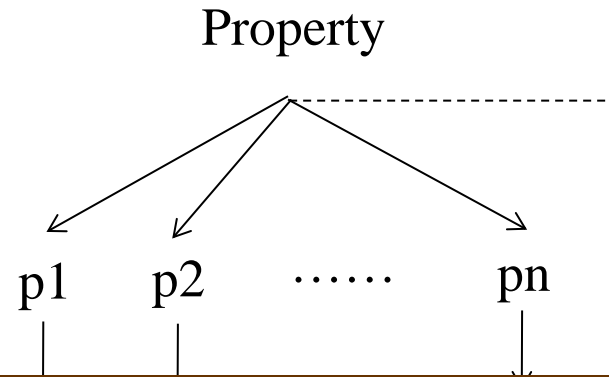
$\Delta$  blue

$\Delta$  green

M. Chen and P. Mishra. **Functional Test Generation using Efficient Property Clustering and Learning Techniques.** *TCAD 2010.*

M. Chen and P. Mishra. **Efficient Decision Ordering Techniques for SAT-based Test Generation.** *DATE 2010.*

# Property Decomposition Techniques



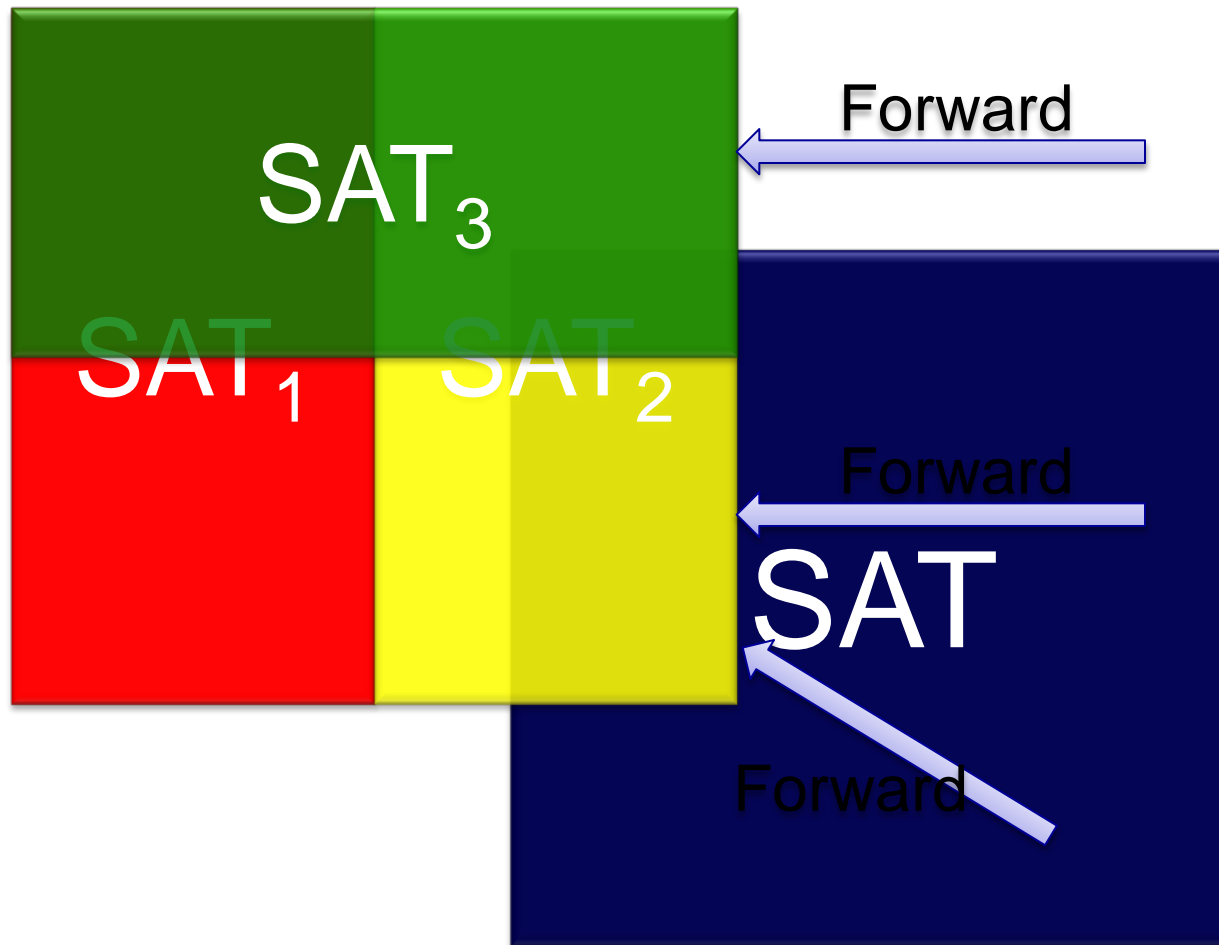
**Problem:** Sub-property decomposition needs expert knowledge?

Test

Koo et al. [Functional Test Generation using Property Decomposition Techniques](#). ACM *TECS*, 2009

M. Chen and P. Mishra. [Decision ordering based property decomposition for functional test generation](#). *DATE*, 2011

# Key Observations



**Problems:** How to achieve the beneficial learning efficiently?

- Which kind of learning can be forwarded?
- How can we achieve and utilize such kinds of learnings?

# Conflict Clause Based Learning

$$\omega_1 = (x_2 \vee x_6 \vee \neg x_4)$$

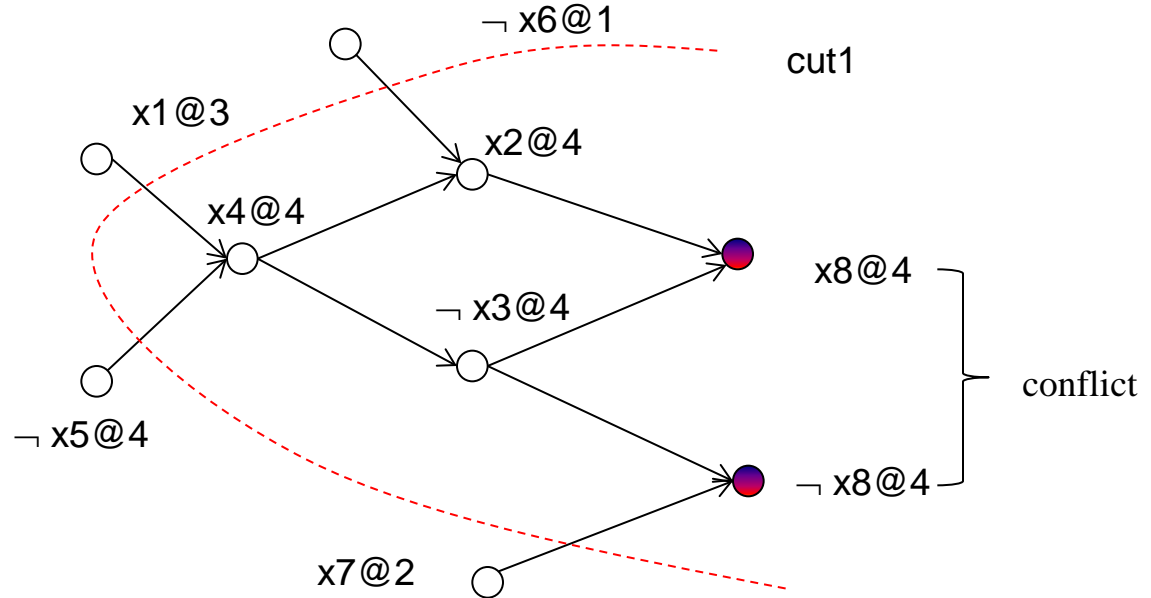
$$\omega_2 = (\neg x_8 \vee x_3 \vee \neg x_7)$$

$$\omega_3 = (\neg x_1 \vee x_4 \vee x_5)$$

$$\omega_4 = (\neg x_3 \vee \neg x_4)$$

$$\omega_5 = (\neg x_2 \vee x_3 \vee x_8)$$

$$\omega_6 : (\neg x_1 \vee x_5 \vee x_6 \vee \neg x_7)$$

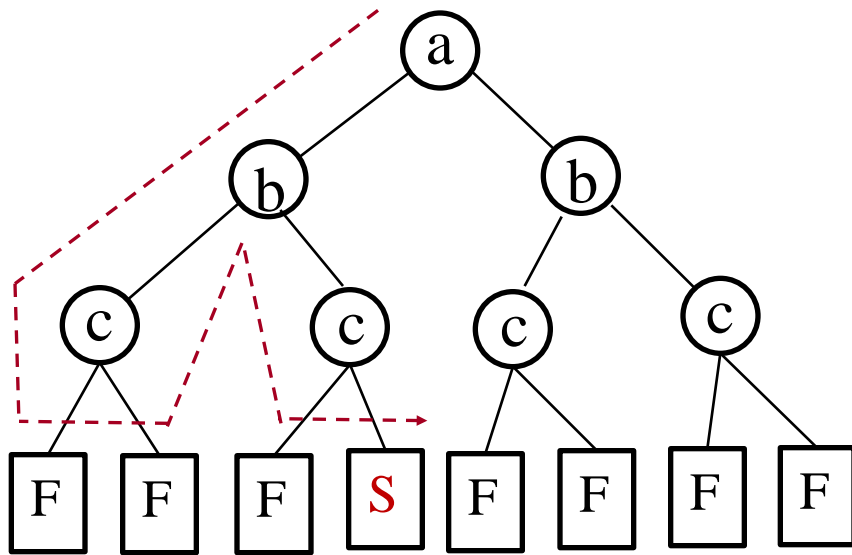


- **Conflict clause can be treated as the knowledge learned during the SAT solving. It is a restriction of the variable assignment.**



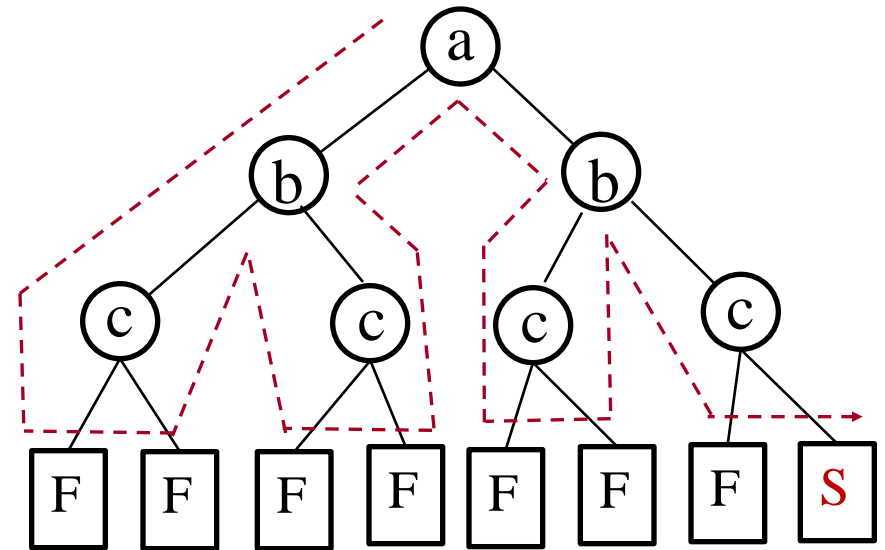
# Decision Ordering Based Learning

SAT 1



Ordering: a, a', b, b', c, c'

SAT 2



Ordering: a, a', b, b', c, c'

*Without Learning, 7 conflicts in SAT2.*

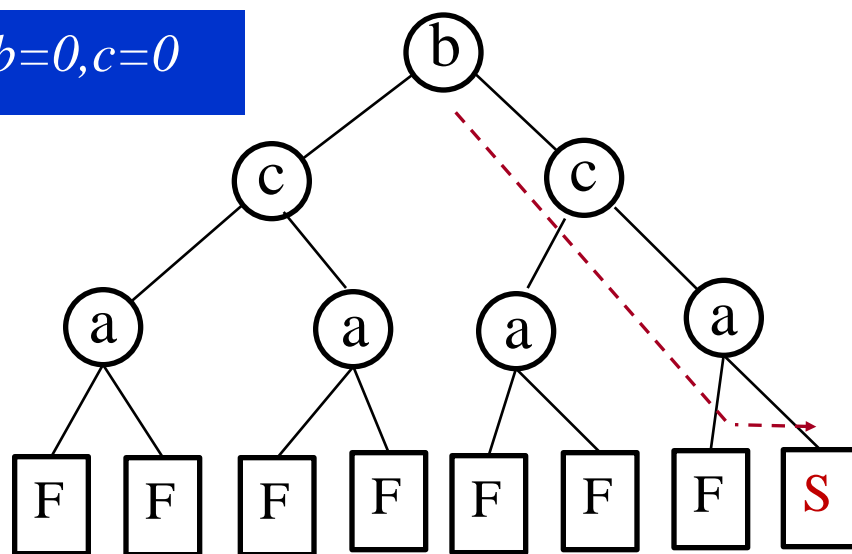
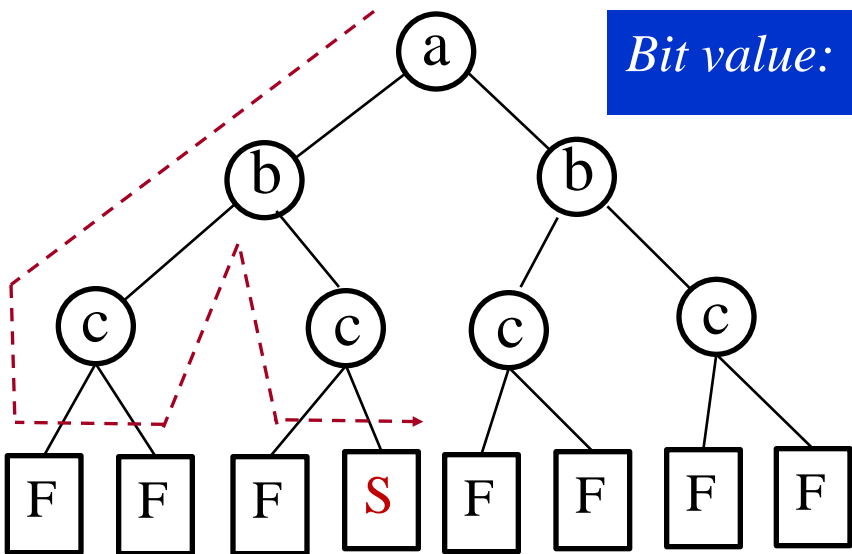
# Decision Ordering Based Learning

SAT 1

Variable order:  $b > c > a$

Bit value:  $a=1, b=0, c=0$

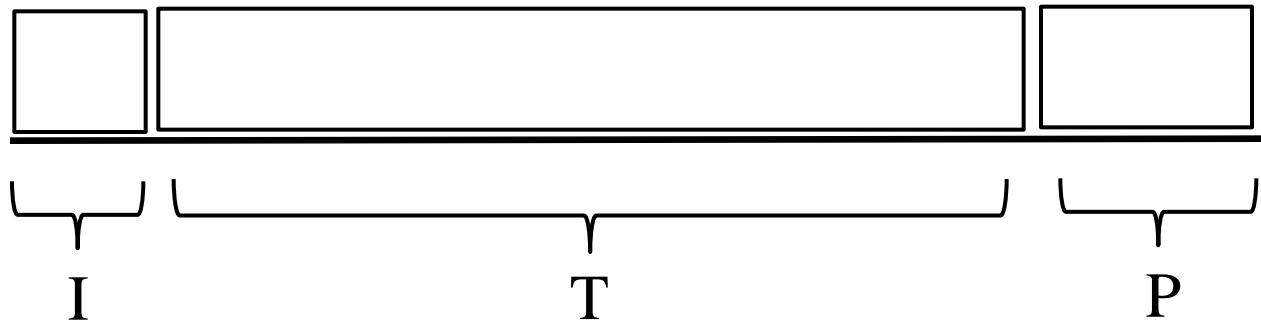
SAT 2



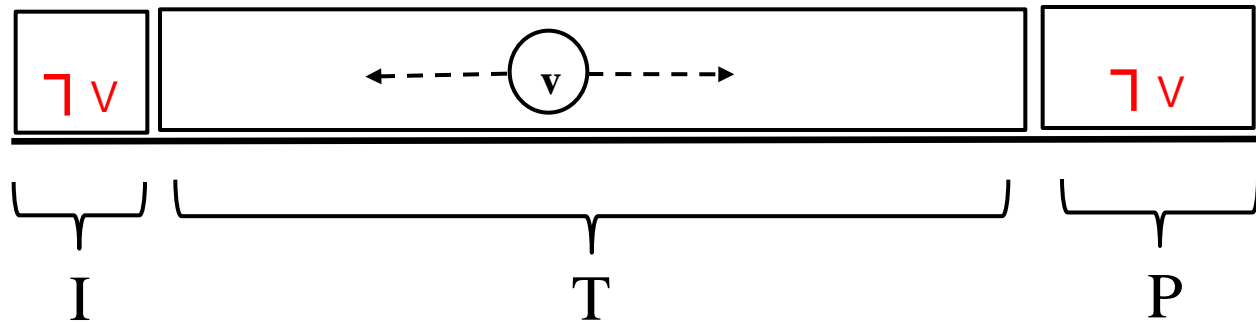
*With bit value + variable order learning, 1 conflict in SAT2.*

# Learn from the Structure of BMC Formulas

$$\Omega(k) = \underbrace{I(S_0)}_I \wedge \underbrace{\bigwedge_{i=0}^{k-1} R(S_i, S_{i+1})}_T \wedge \underbrace{\bigvee_{i=0}^k \neg P(s_i)}_P$$



# Learn from the Structure of BMC Formulas



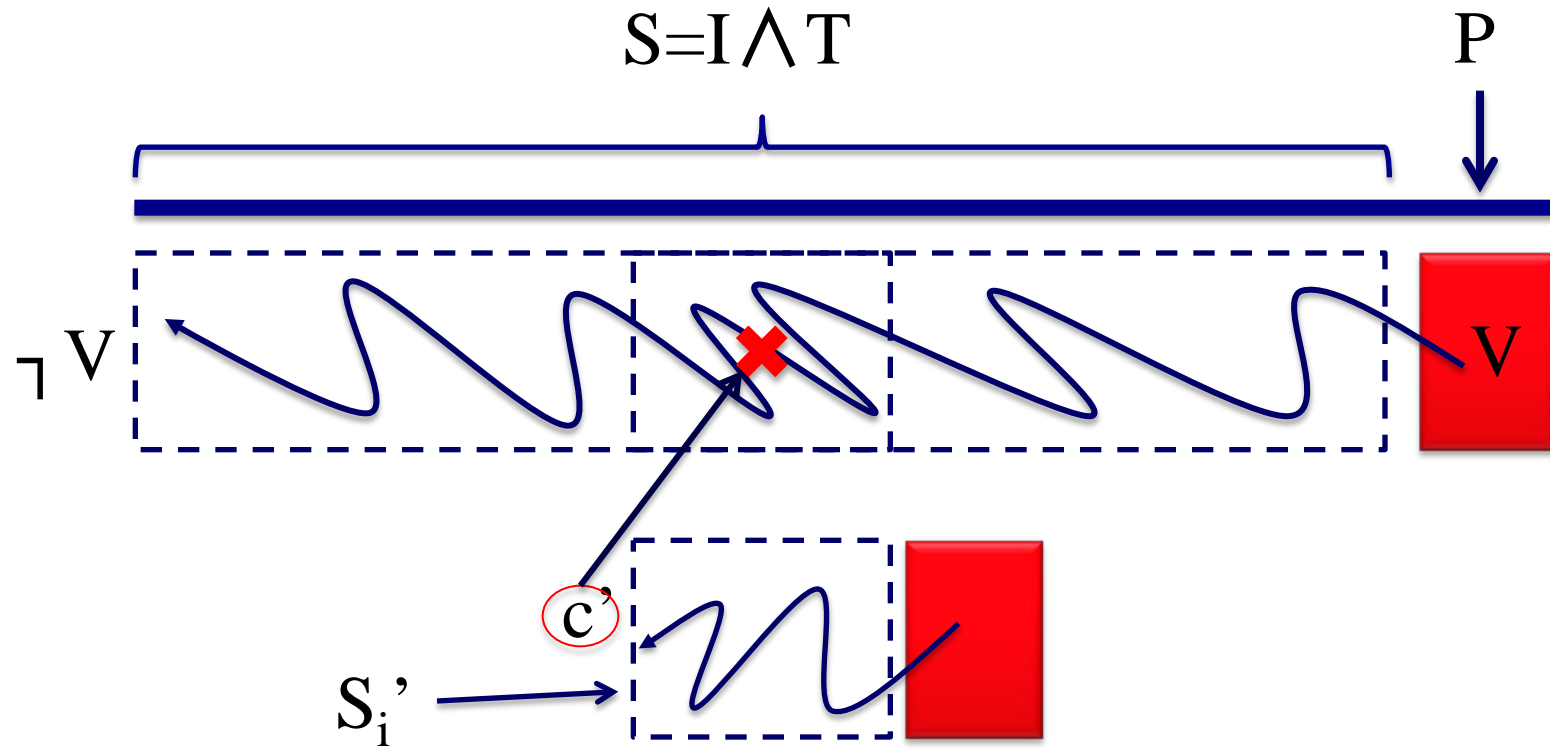
a) A deduction for a transition variable

Reasons for long-distance backtracks:

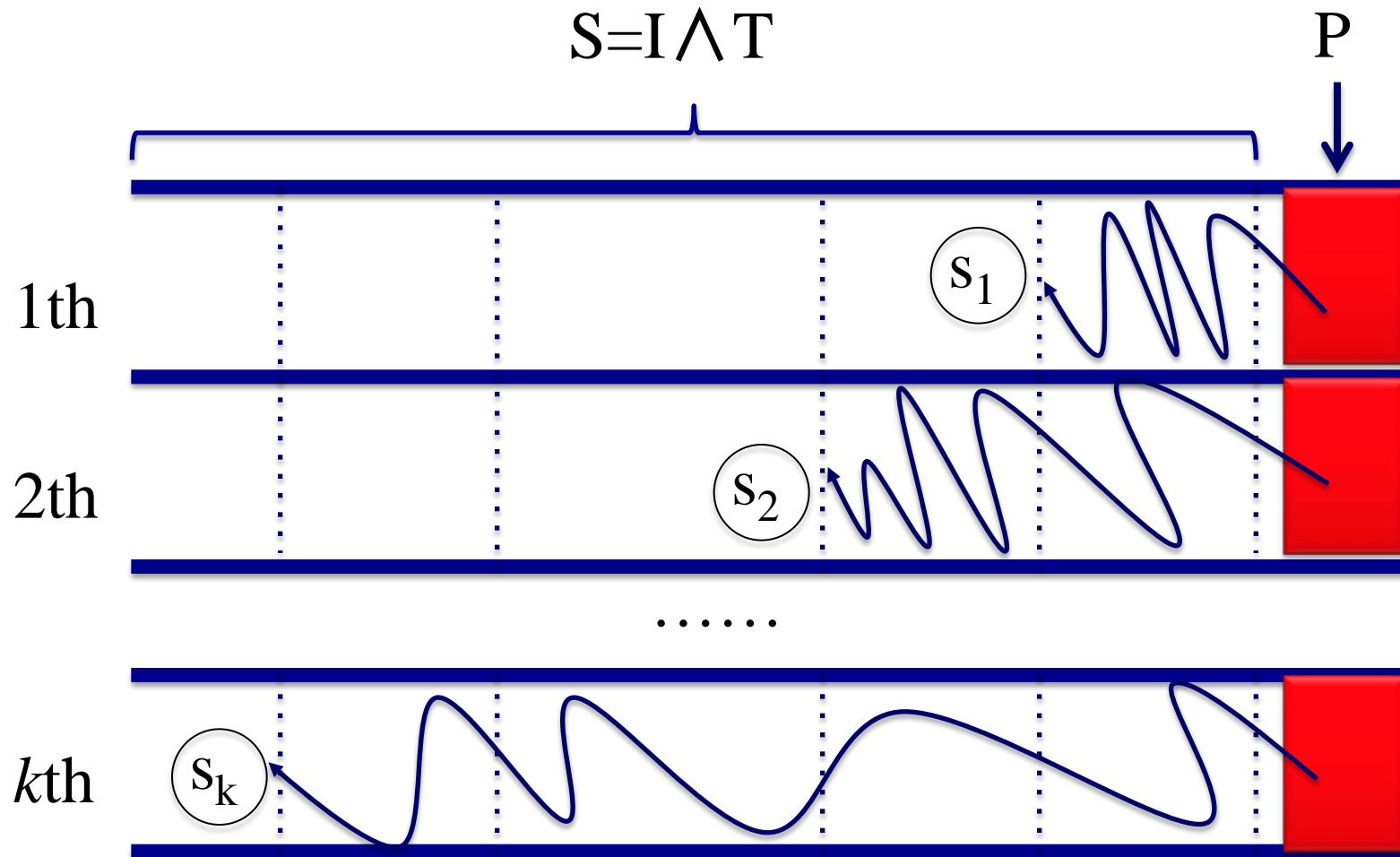
- The constraint imposed by the transition part T is weak.
- A bad decision is made too early but detected too late.

By our observation, **conflict clause** and **decision ordering** are two promising self-learning candidates to address the above two problems.

# Learning from Segmental Partitioning



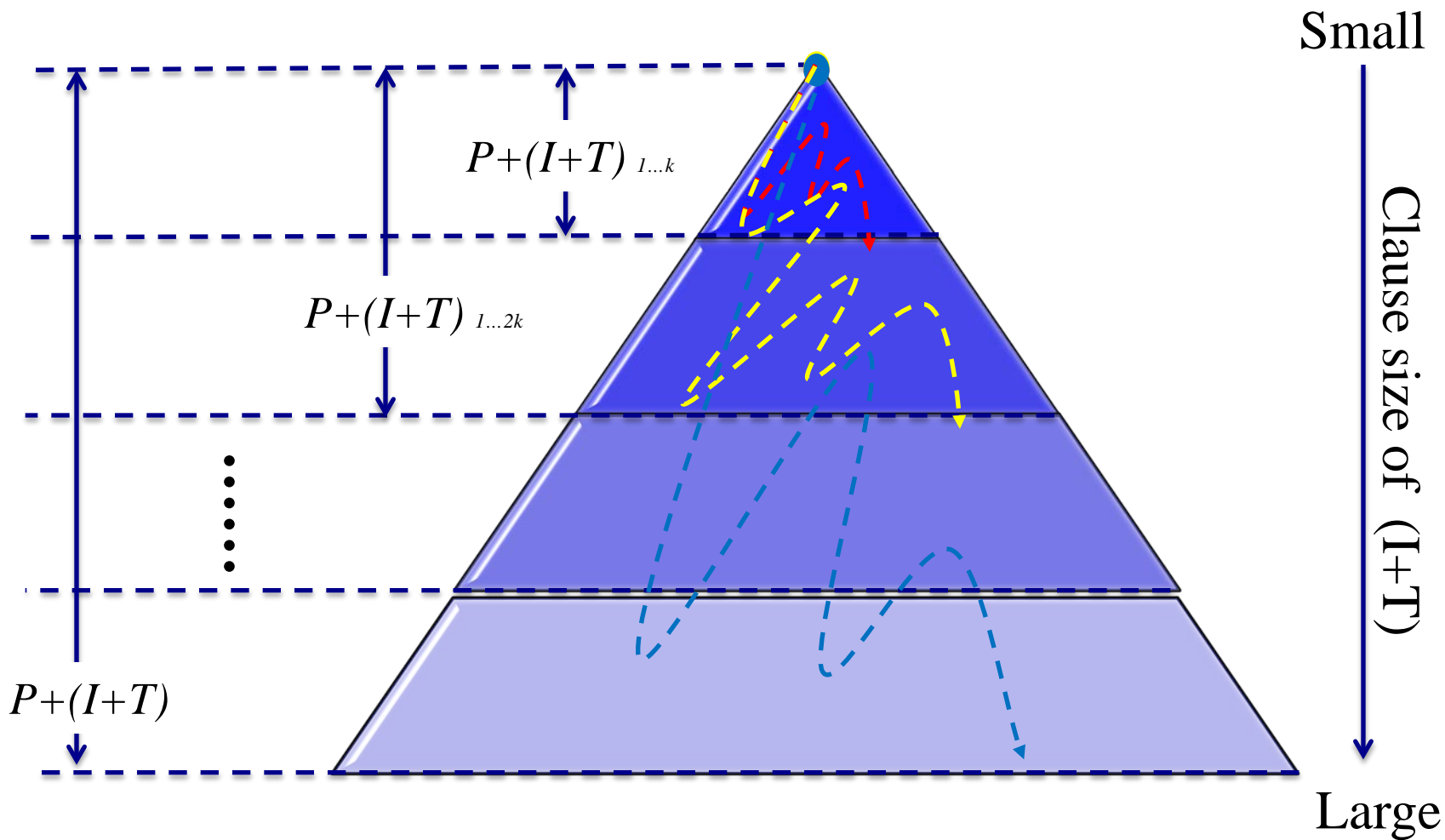
# Learning from Incremental Partitioning



# Learn from the Structure of CNF clauses

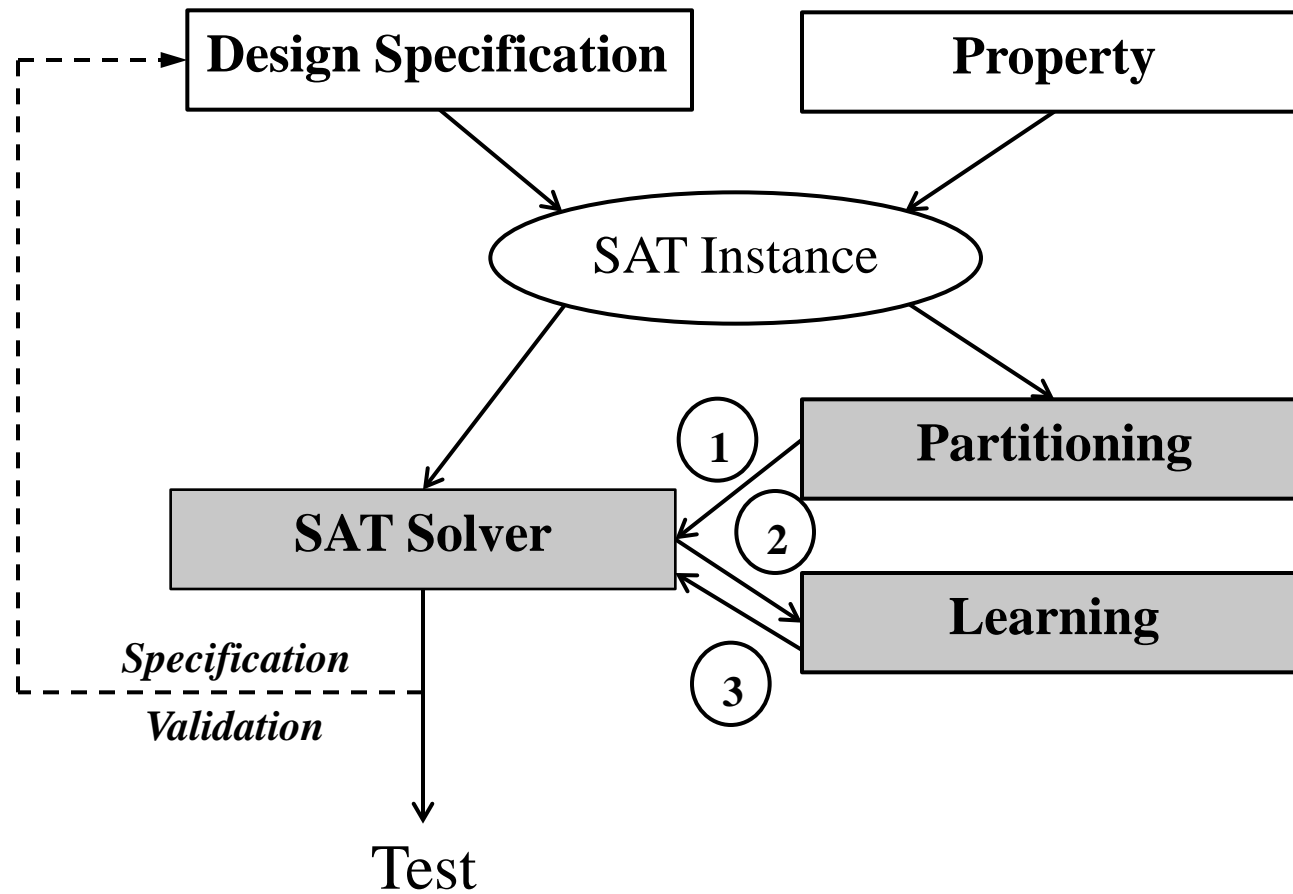
- For a set of small CNF clauses, the impact of a variable decision can be propagate instantly. Only a few decision levels are involved in the searching (avoid long-distance backtracking).
- We take clause size into account to derive high-quality conflict clauses.
  - ◆ A set of small CNF clauses has a high chance to derive small-size conflict clauses.
  - ◆ Smaller conflict clauses can prune more search space.

# Learning from Clause Size Aware Partitioning





# Test Generation using Self-Learning Techniques



# Self-Learning Based Test Generation

- Input:** i) Formal model  $D$  and property  $P$  with the bound  $Bound_p$   
ii) Partitioning type  $type$  and the number of partitions  $n$

**Output:** A test  $tp$  to satisfy the property  $P$

1. Initialize IBucket[1..n] and vStat[1..sz][ ];
2. CNF=BMC(D, P, Bound<sub>p</sub>);
3.  $\{p_1, p_2, \dots, p_n\} = \text{Partition}(\text{CNF}, \text{type}, n)$ ;
4. **for** i is from 1 to n **do**
  - ① (Assign<sub>i</sub>, confi) = SAT( $p_i$ , IBucket[1..i-1], vStat);
  - ② IBucket[i] = confi;
  - ③ **for** j is from 1 to sz **do**
    - a) **if** (assign<sub>i</sub>[j]==0) vStat[j][2]++;
    - b) **else if** (assign<sub>i</sub>[j]==1) vStat[j][1]++;
5. ( $tp, \_$ ) = SAT(CNF, IBucket[1..n] , vStat);
6. Return  $tp$ .

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# Experiments

- The experiments were conducted on a Linux PC with a **3.3GHz** CPU and **4G** RAM.
- We modified the SAT solvers **MiniSAT2.2** and **zChaff** to incorporate our partitioning and self-learning techniques.
- In our experiments, all the SAT instances are divided into **4** partitions by default. For conflict clauses based self-learning, we only forward the conflict clauses whose size is smaller than **9**.

# Case Study 1: DLX+OSES

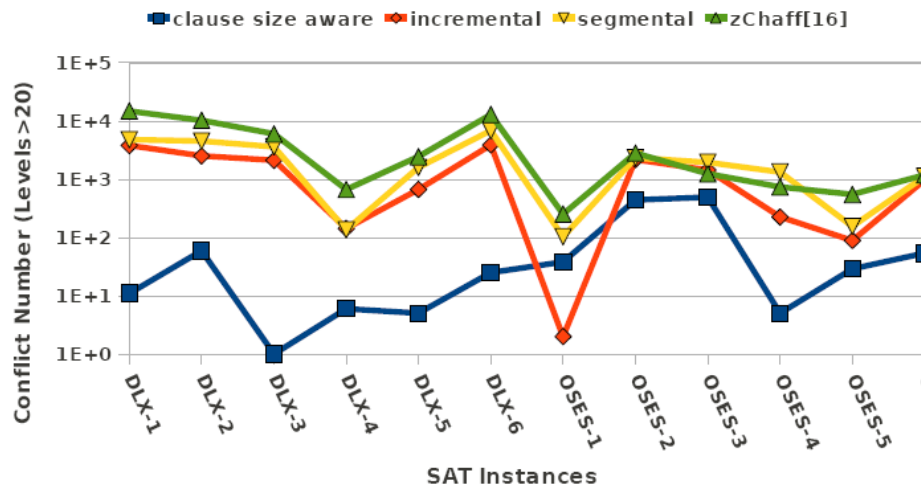
- The benchmark is a set of SAT instances derived from a MIPS processor (DLX), and an online stock exchange system (OSES). All the SAT instances are generated using the tool NuSMV.

SAT Instance	MiniSAT[15] /zChaff[16]	Segmental Partitioning ([15]/[16])			Incremental Partitioning ([15]/[16])			C. S. A. Partitioning ([15]/[16])			Max Speedup
		cls	var	cls+var	cls	var	cls+var	cls	var	cls+var	
DLX-1	1.9/104.5	3.6/72.8	4.3/22.2	<b>3.3</b> /23.0	4.6/133.4	4.9/28.6	3.7/24.6	3.5/23.1	4.3/6.7	3.4/ <b>6.2</b>	0.6/16.9
DLX-2	1.5/58.0	3.5/58.5	3.3/20.8	<b>3.1</b> /19.0	4.3/90.0	4.5/19.1	3.8/13.9	3.8/35.3	4.1/9.5	3.2/ <b>5.7</b>	0.5/10.2
DLX-3	0.8/32.4	1.7/26.3	2.1/12.7	<b>1.6</b> /15.2	2.1/189.2	2.0/8.7	2.0/11.8	1.9/16.9	2.1/5.0	1.8/ <b>3.2</b>	0.5/10.1
DLX-4	0.2/2.1	0.5/2.4	0.6/0.8	0.5/ <b>0.5</b>	0.7/1.5	0.6/0.7	<b>0.5</b> /0.6	0.5/1.4	0.5/0.8	0.5/0.7	0.4/4.2
DLX-5	0.6/7.9	1.3/6.1	1.3/4.2	1.3/3.8	1.4/9.6	1.5/4.9	1.2/2.8	1.1/6.6	1.3/2.9	<b>1.0</b> / <b>2.7</b>	0.6/2.9
DLX-6	1.1/101.3	2.6/105.0	3.0/35.5	2.7/31.0	3.2/106.1	2.8/27.2	2.9/25.6	2.6/71.7	2.6/3.7	<b>2.3</b> / <b>2.9</b>	0.5/34.9
OSES-1	0.6/5.5	<b>0.3</b> /0.6	0.4/18.5	0.4/4.2	0.3/6.3	0.4/1.7	0.3/0.8	0.4/1.0	0.4/ <b>0.5</b>	0.4/0.7	2.0/11.0
OSES-2	0.6/209.3	<b>0.5</b> /80.2	2.1/200.1	0.9/290.6	2.2/131.1	1.6/177.6	1.1/249.0	1.1/246.6	2.3/73.1	1.0/ <b>24.8</b>	1.2/8.4
OSES-3	4.7/121.7	1.7/89.8	9.5/181.5	1.0/238.9	<b>0.9</b> /89.5	2.0/140.8	9.2/269.5	1.9/74.5	1.3/ <b>6.7</b>	5.4/35.3	5.2/18.2
OSES-4	0.9/28.8	3.5/47.3	7.9/91.4	4.0/99.6	4.0/39.0	3.4/45.2	<b>1.0</b> /8.7	5.1/36.4	18.6/ <b>0.8</b>	5.0/0.9	0.9/32.0
OSES-5	0.1/21.8	<b>0.2</b> /20.2	0.3/8.8	0.3/5.2	0.6/12.0	0.3/3.5	0.4/2.7	0.4/21.1	0.3/ <b>0.6</b>	0.3/0.7	0.5/36.3
OSES-6	0.9/53.8	<b>0.3</b> /74.4	0.4/76.5	0.4/67.4	0.7/122.8	0.5/15.2	0.7/78.8	1.2/136.4	1.4/ <b>1.7</b>	1.5/2.3	3.0/31.6

- Since the test generation time using MiniSAT without any learning is small, the extra self-learning does not show significant improvement.

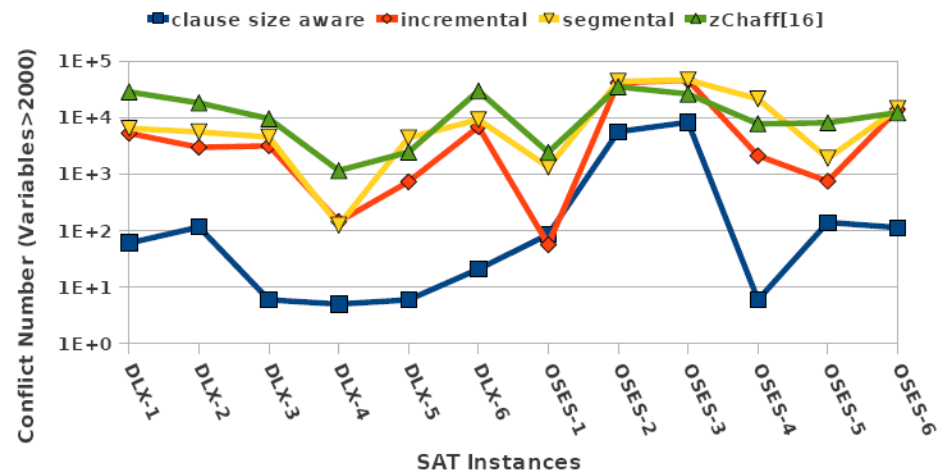
# Case Study 1: DLX+OSES

The conflict which requires a backtrack with  $>20$  decision levels



(a) The statistics of canceled levels

The conflict which requires a cancel of  $>2000$  variable assignments



(b) The statistics of canceled variable assignments

**Indications:** Test generation complexity is significantly reduced in zChaff.

- Reduction of long-distance backtracking
- Reduction of bad decisions

# Case Study 2: PIPE Processor Design

- The benchmark is a set of SAT instances from 10 buggy variants of 12-pipelined processors named PIPE-SAT-1.1.

Table 2: Test Generation Results for PIPE Processors

SAT Instance	MiniSAT[15] /zChaff[16]	Segmental Partitioning ([15]/[16])			Incremental Partitioning ([15]/[16])			C. S. A. Partitioning ([15]/[16])			Max Speedup
		cls	var	cls+var	cls	var	cls+var	cls	var	cls+var	
PIPE1	12/854	28/488	234/761	190/572	8/507	1/242	1/924	26/844	2/7	2/8	12.0/122.0
PIPE2	1/1090	1/2085	1/421	1/1	11/943	1/174	1/217	1/1124	1/11	1/11	1.0/1090.0
PIPE3	15/524	8/879	169/1185	144/1495	8/692	1/521	1/142	16/707	4/276	4/276	15.0/3.7
PIPE4	6/670	36/77	1055/162	1/12	5/311	NA/4	118/4	18/684	2/237	2/236	6.0/167.5
PIPE5	5/395	2/1345	3/2544	2/2613	9/90	2/595	10/1240	16/401	2/55	4/55	2.5/7.2
PIPE6	1/1	1/98	4/106	11/55	1/2	2/122	4/142	1/1	1/1	1/1	1.0/1.0
PIPE7	13/1117	284/505	322/2069	112/1184	450/681	6/1188	4/162	13/1059	4/38	4/39	3.3/29.4
PIPE8	2/73	6/1	44/69	91/61	7/110	NA/75	NA/76	9/73	6/30	11/30	0.3/73
PIPE9	30/3897	32/2522	2/404	2/395	43/421	3/1295	1/964	6/3874	1/1022	1/1020	30.0/9.9
PIPE10	174/907	112/647	672/973	4/497	111/446	2/139	2/118	17/661	4/148	4/147	87.0/7.7

- Both the modified zChaff and MiniSAT shows that our self-learnings can achieve significant improvement.

# Case Study 3: UNSAT PIPE\_000

- We also conducted the experiment on a set of bigger variants of the pipe\_000 benchmarks named PIPE-000-UNSAT-1.1.

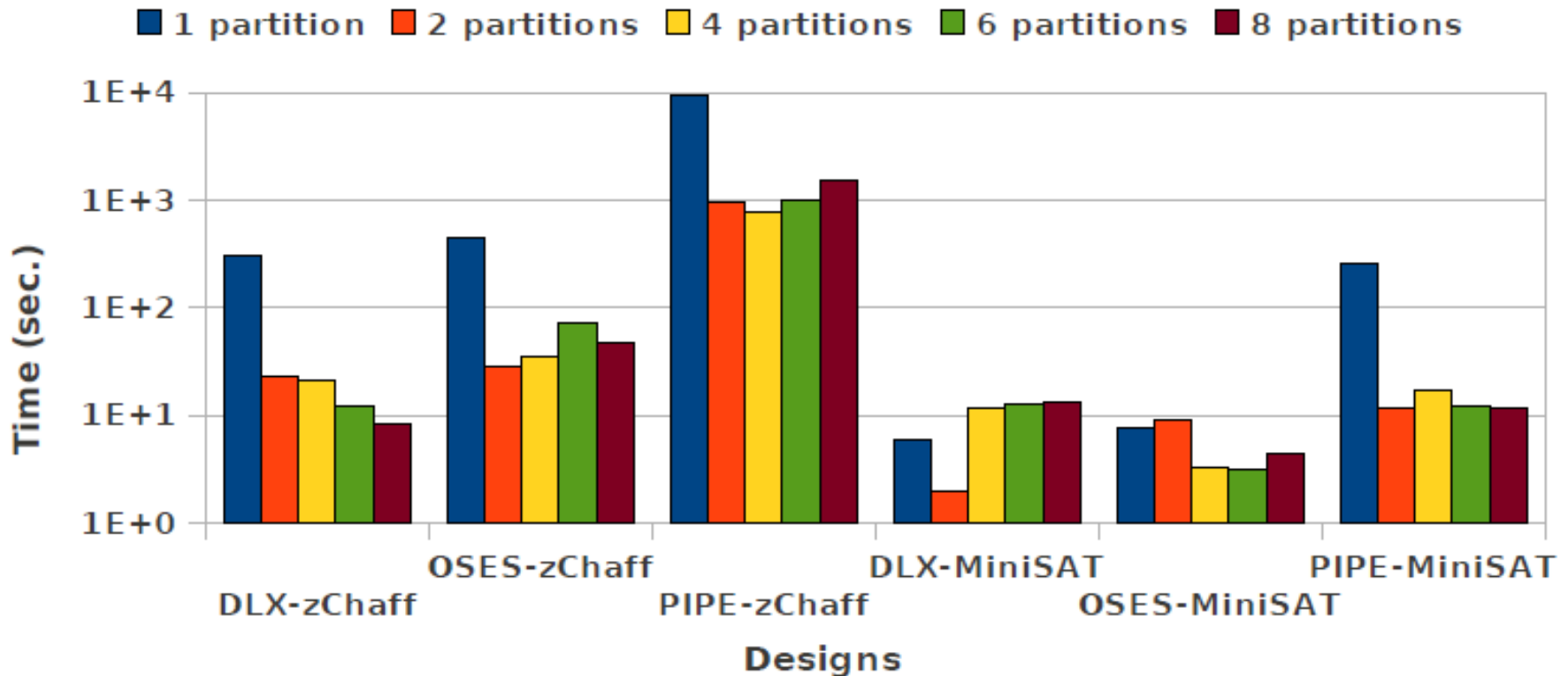
Table 3: SAT Solving Results for UNSAT Instances of PIPE Processors

SAT Instance	MiniSAT[15] /zChaff[16]	Segmental Partitioning ([15]/[16])			Incremental Partitioning ([15]/[16])			C. S. A. Partitioning ([15]/[16])			Max Speedup
		cls	var	cls+var	cls	var	cls+var	cls	var	cls+var	
pipe2-000	0.3/0.06	0.1/ <b>0.05</b>	<b>0.04</b> /0.08	0.05/0.09	0.1/0.06	0.1/0.10	0.1/0.10	0.3/0.08	0.1/0.19	0.1/0.13	7.5/1.2
pipe3-000	10.7/0.8	12.5/0.9	6.7/0.9	5.9/1.1	11.6/1.1	12.5/1.0	8.0/0.9	8.4/ <b>0.8</b>	<b>0.8</b> /1.5	1.2/1.1	13.4/1.0
pipe4-000	94/6	142/4	118/3	111/4	114/3	77/4	197/4	50/6	13/5	<b>10</b> /5	9.4/2.0
pipe5-000	280/18	356/15	64/15	<b>47</b> /14	498/14	NA/12	1065/ <b>11</b>	476/13	51/18	62/21	6.0/1.6
pipe6-000	731/69	NA/65	NA/64	NA/61	279/67	NA/50	NA/ <b>48</b>	645/66	74/78	<b>70</b> /70	10.4/1.4
pipe7-000	1016/266	<b>702</b> /278	NA/285	NA/294	NA/303	NA/ <b>199</b>	NA/208	NA/285	NA/304	NA/295	1.4/1.3
pipe8-000	NA/1107	NA/1330	NA/1083	NA/1104	NA/1387	NA/772	NA/ <b>684</b>	NA/1326	NA/1354	NA/1334	1.4/1.6
pipe9-000	NA/1697	NA/1716	NA/1565	NA/1656	NA/1688	NA/ <b>940</b>	NA/989	NA/1497	NA/2005	NA/1913	NA/1.8

- Interestingly, our approach can also benefit the UNSAT instance checking. We can find that zChaff outperforms MiniSAT in this benchmark, and our self-learning techniques can achieve an up to 13.4 times improvement using MiniSAT and 2 times improvement using zChaff.



# Evaluation of the number of partitions



## Indications:

- For zChaff, the methods using 4 partitions show a better performance for these three benchmarks.
- For MiniSAT, the approaches using 2 partitions or 4 partitions are good enough for test generation.

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# Conclusions

- Functional validation is a major bottleneck
  - ◆ SAT-based approaches are promising for automated test generation.
- Proposed efficient self-learning techniques for automated generation of directed tests
  - ◆ Investigated two kinds of learning objects.
  - ◆ Developed three learning-oriented partitioning heuristic methods.
- Successfully applied on both hardware and software designs
  - ◆ Significant reduction in test generation time.



**Thank you !**